

# *Extracting Flavor from Quiver Gauge Theories*

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Based on collaboration with Yaron Antebi and Yossi Nir, [Phys. Rev. D73,075009].

# Motivation

- The current information on the (dimensionless parameters of the) neutrino sector:

$$\tan^2\theta_{23} \sim 0.53-1.89$$

$$\tan^2\theta_{12} \sim 0.31-0.61$$

$$|U_{e3}| \leq 0.17$$

$$\sqrt{\Delta m_{21}^2 / |\Delta m_{32}^2|} \sim 0.17-0.20$$

- In contrast to the quarks and charged leptons, the parameters above are not particularly small nor hierarchical.
- Thus it could be that the neutrino sector is anarchical. [Hall, Murayama, Weiner (2000)]
- This can be tested by measuring the mass scales,  $m_i$  and the mixing angle  $\theta_{13}$ .

## So why are neutrinos so special? Why are they flavor blind?

- It is possible to generate such anarchy through the FN mechanism (approximate symmetry).
- But the FN mechanism has limitations: there are many other FN models which do not predict anarchy.

Can we motivate one model over others? Is there a framework which predicts anarchy in the neutrino sector?

- In this talk we'll consider a string motivated class of models: **quiver gauge theories**.
- Certain class of (heterotic) string motivated FN models were investigated in the past and found to be more constraining.

[Ibanez, Ross (1994)]  
[Binetruy, Ramond (1995)]  
[Elwood, Irges, Ramond (1997),(1998)]  
[Binetruy, Lavignac, Ramond (1996)]  
[Dreiner, Murayama, Thormeier (2005)]

## *To Make a Long Story Short:*

The FN mechanism within quiver gauge theories is more predictive.

Under mild assumptions, anarchy is predicted.



A bottom-up approach in which phenomenology constrains a certain class of string theories.

# The FN Mechanism

- Provides an explanation to the flavor puzzle.

[Froggatt, Nielsen (1979)]  
[Leurer, Nir, Seiberg (1993)]

- $U(1)_{\text{FN}}$  horizontal symmetry which is spontaneously broken by a VEV of a scalar field  $S$ ,

$$\langle S \rangle / M_V = \varepsilon \ll 1.$$

- $M_V$  is the scale at which the breaking is communicated to the visible sector through massive fields in vector-like representations of the gauge group.
- The charges of the various fields dictate the parametric suppression in  $\varepsilon$ .

- For the FN mechanism, one chooses the small parameter,  $\varepsilon$ , and a set of charges. These dictate the parametric suppression of the various operators.
- Thus the mechanism is limited:
  - The value of the small parameter is arbitrary.
  - The charges of the various fields are not predicted.
  - No information on the  $O(1)$  parameters is given.
- To demonstrate, consider for example the SU(5) models:

$$\begin{aligned}
 \text{⤴ } (10_i) &= (2,1,0) & M_u &= \langle H_u \rangle \begin{pmatrix} \varepsilon^4 & \varepsilon^3 & \varepsilon^2 \\ \varepsilon^3 & \varepsilon^2 & \varepsilon \\ \varepsilon^2 & \varepsilon & 1 \end{pmatrix} & M_d &= \langle H_d \rangle \begin{pmatrix} \varepsilon^2 & \varepsilon^2 & \varepsilon^2 \\ \varepsilon & \varepsilon & \varepsilon \\ 1 & 1 & 1 \end{pmatrix} & M_\nu &= \frac{\langle H_u \rangle^2}{M} \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} & \varepsilon &= 0.05 \\
 \text{⤴ } (\bar{5}_i) &= (0,0,0)
 \end{aligned}$$

$$\text{⤴ } (H_u) = \text{⤴ } (H_d) = 0$$

$$\text{⤴ } (S) = -1$$

Different Neutrino Structure

$$\begin{aligned}
 \text{⤴ } (10_i) &= (4,2,0) & M_u &= \langle H_u \rangle \begin{pmatrix} \varepsilon^8 & \varepsilon^6 & \varepsilon^4 \\ \varepsilon^6 & \varepsilon^4 & \varepsilon^2 \\ \varepsilon^4 & \varepsilon^2 & 1 \end{pmatrix} & M_d &= \langle H_d \rangle \begin{pmatrix} \varepsilon^5 & \varepsilon^5 & \varepsilon^4 \\ \varepsilon^3 & \varepsilon^3 & \varepsilon^2 \\ \varepsilon & \varepsilon & 1 \end{pmatrix} & M_\nu &= \frac{\langle H_u \rangle^2}{M} \begin{pmatrix} \varepsilon^2 & \varepsilon^2 & \varepsilon \\ \varepsilon^2 & \varepsilon^2 & \varepsilon \\ \varepsilon & \varepsilon & 1 \end{pmatrix} & \varepsilon &= 0.23 \\
 \text{⤴ } (\bar{5}_i) &= (1,1,0)
 \end{aligned}$$

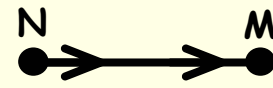
# Quiver Gauge Theories

- Quiver gauge theories arise as low energy effective theories on D-branes placed on singular manifolds.

[Douglas, Moore (1996)]  
 [Johnson, Myers (1996)]  
 [Lawrence, Nekrasov, Vafa (1998)]

- An extended quiver diagram is a graph which efficiently describes the gauge theory for oriented strings:


$\bullet^N = U(N), SO(N) \text{ or } SP(N)$

 =  $(N, \bar{M})$

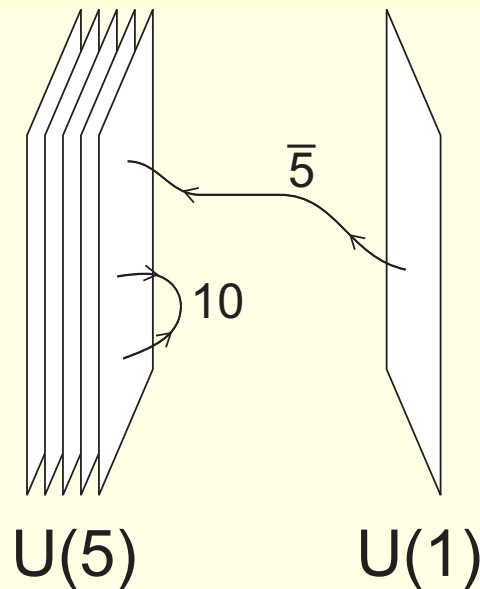
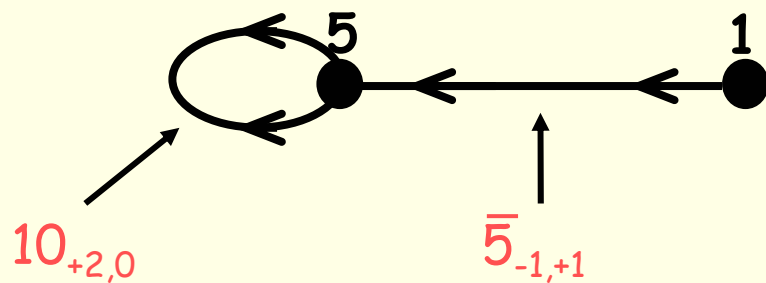
 = Adj

 =  $(\bar{N}, \bar{M})$

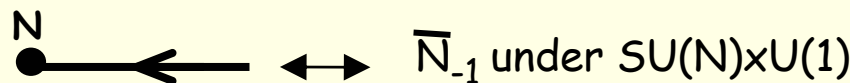
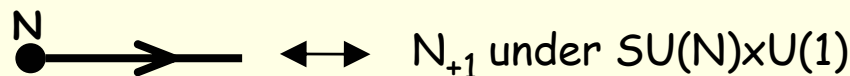
 =  $(N, M)$

 = Symmetric or Antisymmetric of  $N \times N$

Consider as an example,  $U(5) \times U(1)$  theory:



For each  $U(N) = SU(N) \times U(1)$  factor, the charge under the  $U(1)$  part of the gauge group is dictated by the representation of the non-abelian part.





- ⊗ The U(1)s pose problems to model building: For example in the U(5)=SU(5)×U(1)

$$\odot = H_d \cdot 10 \cdot \bar{5} + H_u \cdot 10 \cdot 10 + \frac{H_u \cdot H_u \cdot \bar{5} \cdot \bar{5}}{M}$$

the up-type Yukawa couplings cannot be turned on.

- ⊗ Such problems occur already in the SM and in GUT models which embed it.

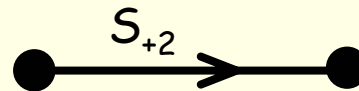
- ⊗ There are three possible solutions:

1. Extend the particle content.
2. Spontaneously break the U(1)  $\rightarrow$  Z<sub>N</sub> by a composite field.
3. The anomalous U(1) is broken by non-perturbative effects.

[Ibanez, Marchesano, Rabadan (2001)]

## *Embedding the FN Mechanism*

- ⊙ Within the quiver framework, the theory is more predictive.
- ⊙ Horizontal symmetry through the U(1)s.
- ⊙ Relation between Abelian and non-Abelian charges strongly restricts possible FN charges.
- ⊙ In particular under any U(1), fields can be charged at most  $\pm 2$ .



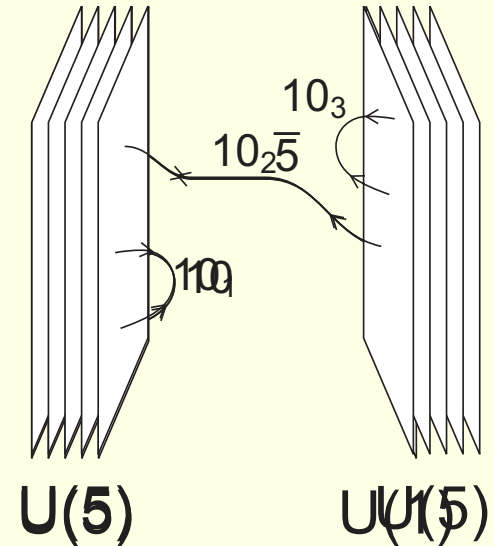
- ⊙ The largest possible suppression for a  $U(1)_{\text{FN}}$  is therefore  $\varepsilon^3$ .

# $SU(5)$ and Neutrino Anarchy

- It is not trivial to generate hierarchy in the up sector:

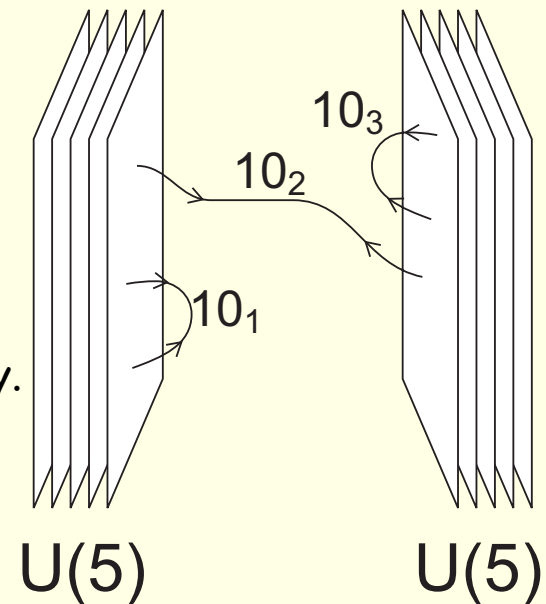
All  $10$ -plets have the same FN charge  $\rightarrow$  No hierarchy!

- We must therefore consider extended gauge groups.



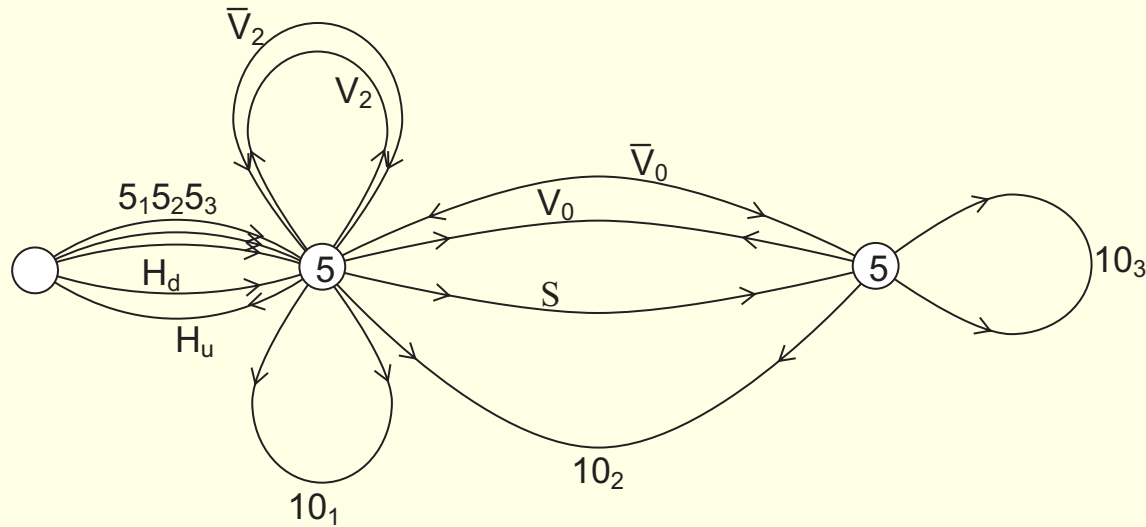
- This is generic in this framework:  $S$  breaks some of the non-abelian symmetry and therefore, *FN requires an extended gauge group*.
- We therefore assume the simplest  $SU(5) \times SU(5)$  with a single FN field.

- $S$  is a bifundamental,  $(\mathbf{5}, \bar{\mathbf{5}})$ . After obtaining a VEV,  $S$  breaks the  $SU(5) \times SU(5) \rightarrow SU(5)_{\text{diag}}$ .
- $S$  is charged  $(1, -1)$  under  $U(1) \times U(1)$ . Therefore  $U(1)_{\text{FN}} = U(1)_L - U(1)_R$
- The 10-plets can have one of three possible charges:  $(2, 0)$ ,  $(1, 1)$ ,  $(0, 2)$  under the  $U(1) \times U(1)$ . To explain the hierarchy in the up-sector each generation must have a different representation.
- The 5-plets can have one of two charges:  $(-1, 0)$ ,  $(0, -1)$  under  $U(1) \times U(1)$ . Thus at least two generations have similar charges and therefore:
  - The neutrino sector must admit (at least) quasi-anarchy.
  - $m_s/m_b \approx |V_{cb}|$
- To have the correct hierarchy in the down sector one finds that all 5-plets must have the same charge!



In this framework anarchy in the neutrino sector is predicted.

# A Simple $SU(5)$ Quiver

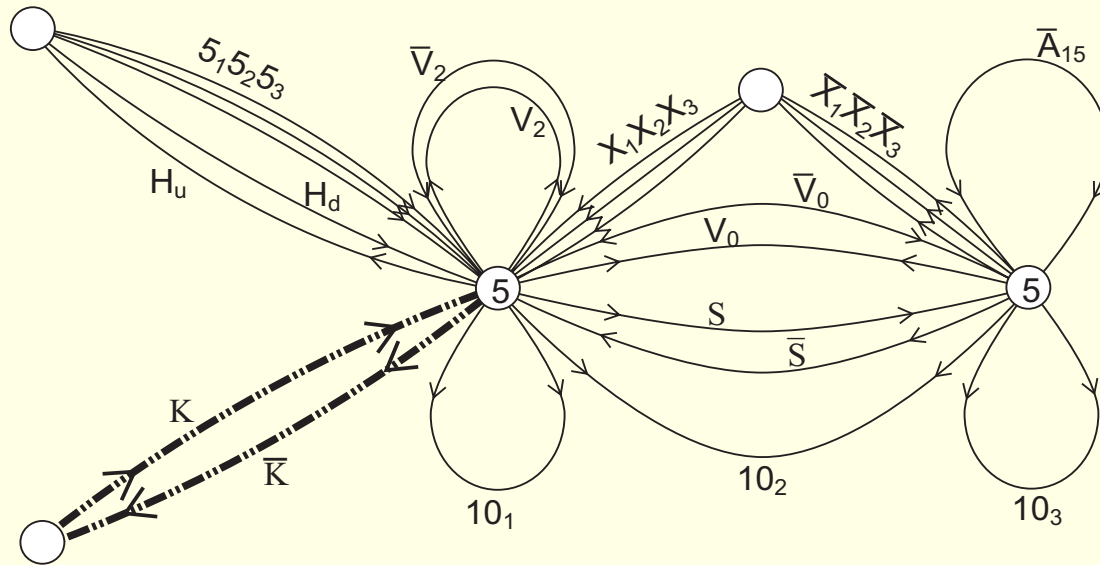


- The above quiver correctly reproduce hierarchy in the quarks and charged leptons and predicts anarchy for the neutrinos.
- It is unique.

# Summary

- 1) The FN mechanism within quiver gauge theories are much more restrictive:
  - 1) There is a relation between Abelian and non-Abelian charges.
  - 2) The FN framework requires product groups.
- 2) In the SU(5) scenario, anarchy in the neutrino sector is predicted.
- 3) The predictive power allows to experimentally constrain classes of string models.
- 4) A generic problem in quiver models: the U(1) factors do not allow all couplings.  
Solution: non-perturbative effects or extended particle content.

# A Complete $SU(5)$ Model



- The above generates the correct hierarchy in quarks and charged leptons and predicts anarchy for the neutrinos.
- It is anomaly free.
- $K$  break the  $U(1)_{L+R}$  spontaneously.